

Designation of Cutting Tools

By designation or nomenclature of a cutting tool is meant the designation of the shape of the cutting part of the tool. The following systems to designate the cutting tool shape which are widely used are:

- Tool in Hand System
- Machine Reference System or American Standard Association (ASA) System
- Tool Reference System
 - Orthogonal Rake System (ORS)
 - Normal Rake System (NRS)
- Maximum Rake System (MRS)
- Work Reference System (WRS)

Tool Reference System

The references from which the tool angles are specified are the

- Reference plane (π_R)
- Machine longitudinal plane (π_x)
- Machine transverse plane (π_y)
- Principal cutting plane (π_c)
- Orthogonal plane (π_o) and
- Normal plane (π_n)

The reference plane (π_R) is the plane perpendicular to the cutting velocity (V_c). The machine longitudinal plane (π_x) is the plane perpendicular to π_R and taken in the direction of feed (longitudinal feed). The machine transverse plane (π_y) is the plane perpendicular to both π_R and π_x or plane perpendicular to π_R and taken in the direction of cross feed. The principal cutting plane (π_c) is the plane perpendicular to π_R and containing the principal cutting edge. The orthogonal plane (π_o) is the plane perpendicular to π_R and π_c . The normal plane (π_n) is perpendicular to the principal cutting edge.

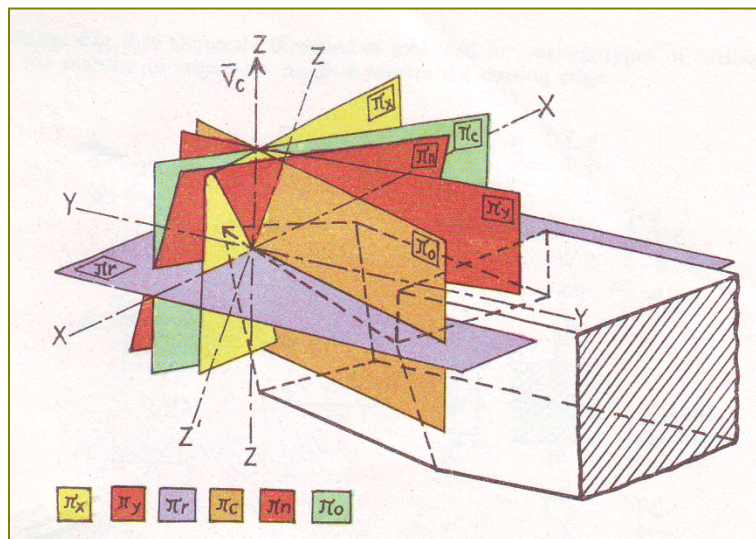
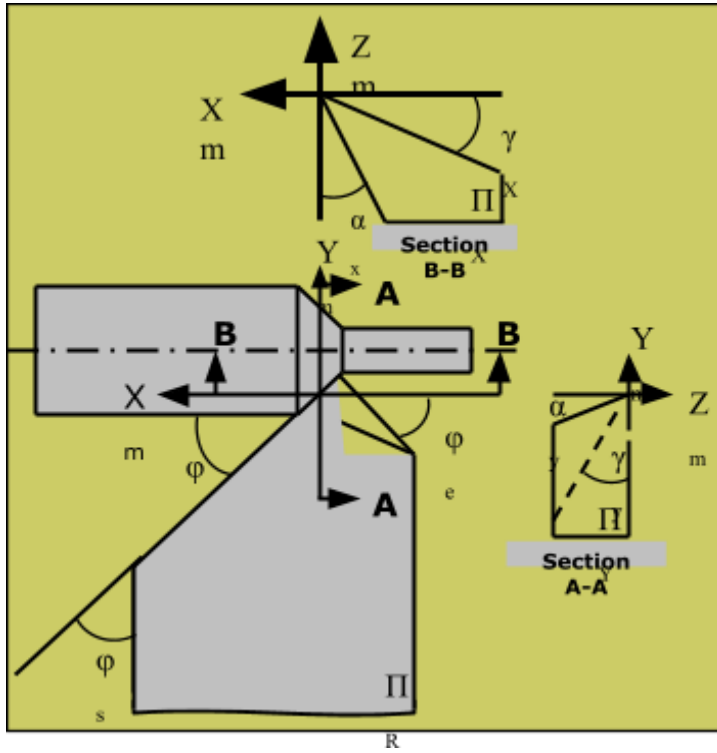


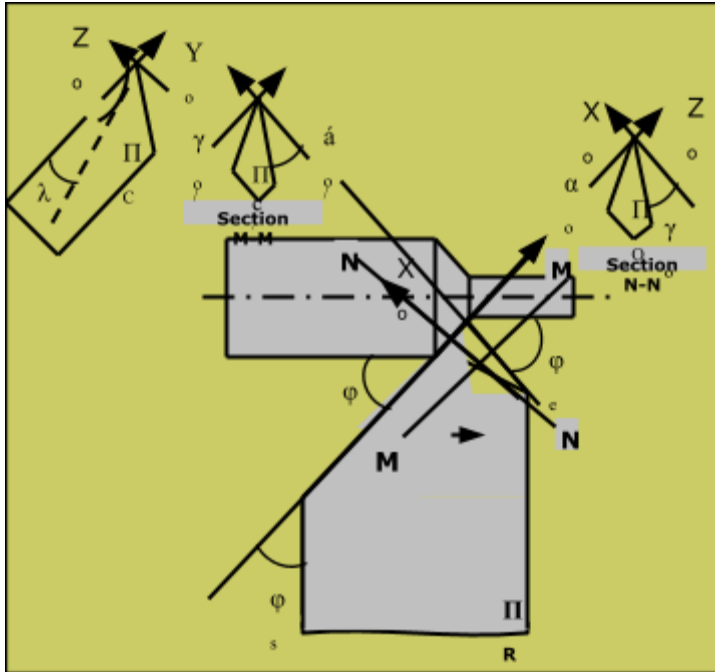
Fig 3.6

American Standard Association System



Tool Character						
γ_v	γ_x	α_v	α_x	ϕ_e	ϕ_s	r
5°	10°	7°	8°	20°	30°	1/32
γ_v	Back rake angle					
γ_x	Side rake angle					
α_v	Back or end clearance angle					
α_x	Side clearance angle					
ϕ_e	Auxiliary or End cutting edge angle					
ϕ_s	Side cutting edge angle (90°- ϕ)					
r	Nose radius (inch)					

Orthogonal Rake System (ORS)



Tool Character						
λ	γ_0	α_0	α_0'	ϕ_e	ϕ	r
5°	10°	7°	8°	20°	30°	0.8 mm
λ	Inclination angle					
γ_0	Orthogonal rake angle					
α_0	Orthogonal clearance angle					
α_0'	Auxiliary orthogonal clearance angle					
ϕ_e	Auxiliary or End cutting edge angle					
ϕ	Principal cutting edge angle ($90-\phi_s$)					
r	Nose radius (mm)					

Interconversion Between ASA and ORS

Interrelations can be established between ASA and ORS and vice versa. Various methods are used for developing such interrelationships such as

- Method of projection
- Method of slopes
- Method of master line
- Circle diagram
- Vector methods, etc.

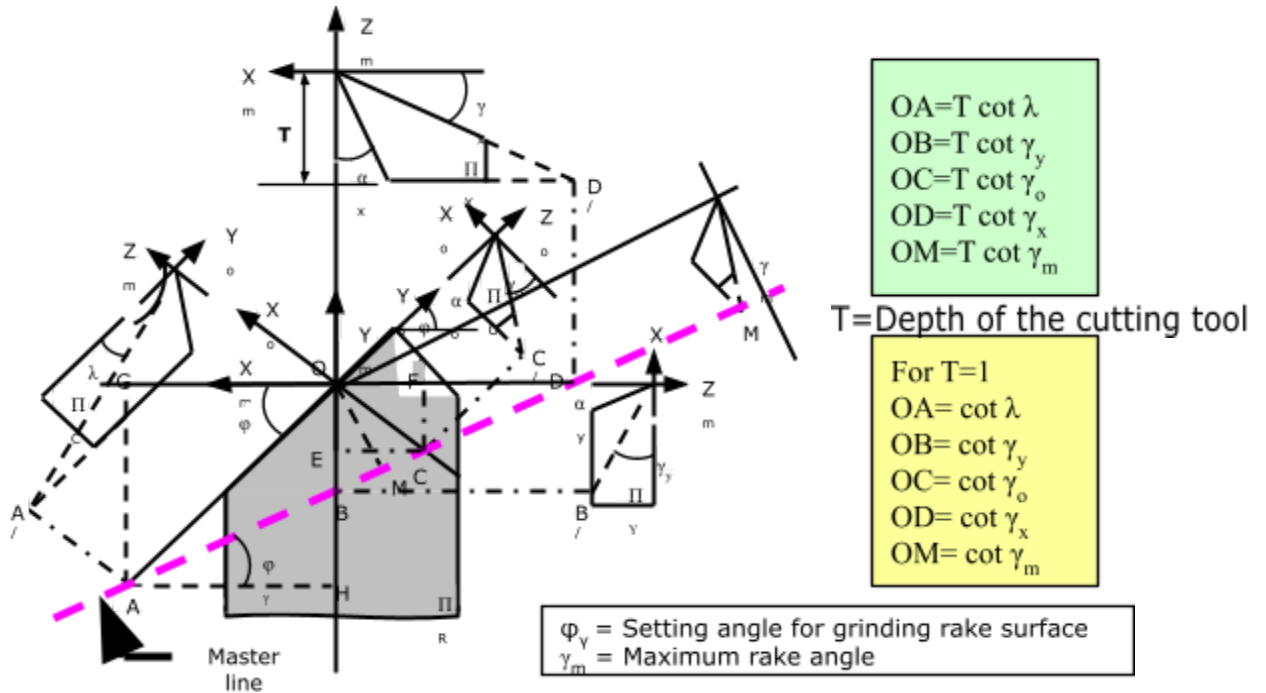


Fig 3.6

- Prove the followings by master line methods for a single point cutting tool.

(i) $\tan \gamma_o = \tan \gamma_x \sin \phi + \tan \gamma_y \cos \phi$

(ii) $\tan \lambda = -\tan \gamma_x \cos \phi + \tan \gamma_y \sin \phi$

(iii) $\tan \gamma_x = \tan \gamma_o \sin \phi - \tan \lambda \cos \phi$

(iv) $\tan \gamma_y = \tan \gamma_o \cos \phi + \tan \lambda \sin \phi$

(v) $\tan \gamma_m = \sqrt{\tan^2 \gamma_o + \tan^2 \lambda}$

(vi) $\phi_\gamma = \phi - \tan^{-1} \left(\frac{\tan \lambda}{\tan \gamma_o} \right)$

ϕ_γ = Setting angle for grinding rake surface
 γ_m = Maximum rake angle

$$\tan \gamma_o = \tan \gamma_x \sin \phi + \tan \gamma_y \cos \phi$$

From Figure $\Delta OBD = \Delta OBC + \Delta OCD$

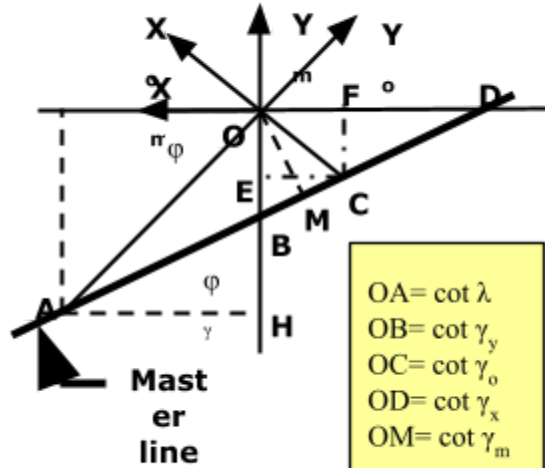
$$\frac{1}{2} OB \cdot OD = \frac{1}{2} OB \cdot CE + \frac{1}{2} OD \cdot CF$$

$$\frac{1}{2} OB \cdot OD = \frac{1}{2} OB \cdot OC \sin \phi + \frac{1}{2} OD \cdot OC \cos \phi$$

Dividing on both sides by $\frac{1}{2} OB \cdot OC \cdot OD$

$$\frac{1}{OC} = \frac{\sin \phi}{OD} + \frac{\cos \phi}{OB}$$

$$\tan \gamma_o = \tan \gamma_x \sin \phi + \tan \gamma_y \cos \phi$$



$$\begin{aligned} OA &= \cot \lambda \\ OB &= \cot \gamma_y \\ OC &= \cot \gamma_o \\ OD &= \cot \gamma_x \\ OM &= \cot \gamma_m \end{aligned}$$

$$\tan \lambda = -\tan \gamma_x \cos \phi + \tan \gamma_y \sin \phi$$

From Figure $\Delta OAD = \Delta OAB + \Delta OBD$

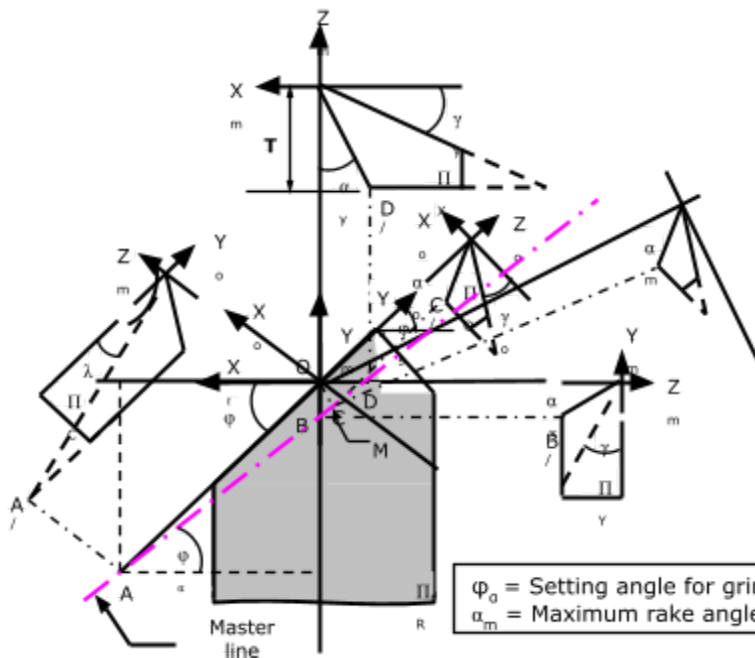
$$\frac{1}{2} OD \cdot AG = \frac{1}{2} OB \cdot AH + \frac{1}{2} OD \cdot OD$$

$$\frac{1}{2} OD \cdot OA \cdot \sin \phi = \frac{1}{2} OB \cdot OA \cos \phi + OB \cdot OD$$

Dividing on both sides by $\frac{1}{2} OA \cdot OB \cdot OD$

$$\frac{\sin \phi}{OB} = \frac{\cos \phi}{OD} + \frac{1}{OA}$$

$$\tan \lambda = -\tan \gamma_x \cos \phi + \tan \gamma_y \sin \phi$$



$$\begin{aligned} OA &= T \cot \lambda \\ OB &= T \tan \alpha_y \\ OC &= T \tan \alpha_o \\ OD &= T \tan \alpha_x \\ OM &= T \tan \alpha_m \end{aligned}$$

T = Depth of the cutting tool

$$\begin{aligned} \text{For } T=1 \\ OA &= \cot \lambda \\ OB &= \tan \alpha_y \\ OC &= \tan \alpha_o \\ OD &= \tan \alpha_x \\ OM &= \tan \alpha_m \end{aligned}$$

ϕ_o = Setting angle for grinding principal rake surface
 α_m = Maximum rake angle

• Prove the followings by master line methods for a single point cutting tool.

(i) $\cot \alpha_o = \cot \alpha_x \sin \phi + \cot \alpha_y \cos \phi$

(ii) $\tan \lambda = -\cot \alpha_x \cos \phi + \cot \alpha_y \sin \phi$

(iii) $\cot \alpha_x = \cot \alpha_o \sin \phi - \tan \lambda \cos \phi$

(iv) $\cot \alpha_y = \cot \alpha_o \cos \phi + \tan \lambda \sin \phi$

(v) $\cot \alpha_m = \sqrt{\cot^2 \alpha_o + \tan^2 \lambda}$

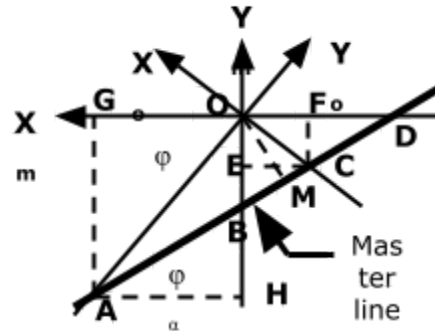
(vi) $\phi_\alpha = \phi - \tan^{-1} \left(\frac{\tan \alpha_o}{\cot \lambda} \right)$

$\cot \alpha_o = \cot \alpha_x \sin \phi + \cot \alpha_y \cos \phi$
 From Figure $\Delta OBD = \Delta OBC + \Delta OCD$
 $\frac{1}{2}OB \cdot OD = \frac{1}{2}OB \cdot CE + \frac{1}{2}OD \cdot CF$
 $\frac{1}{2}OB \cdot OD = \frac{1}{2}OB \cdot OC \sin \phi + \frac{1}{2}OD \cdot OC \cdot \cos \phi$
 Dividing on both sides by $\frac{1}{2}OB \cdot OC \cdot OD$
 $\frac{1}{OC} = \frac{\sin \phi}{OD} + \frac{\cos \phi}{OB}$

$$\cot \alpha_o = \cot \alpha_x \sin \phi + \cot \alpha_y \cos \phi$$

$\tan \lambda = -\cot \alpha_x \cos \phi + \cot \alpha_y \sin \phi$
 From Figure $\Delta OAD = \Delta OAB + \Delta OBD$
 $\frac{1}{2}OD \cdot AG = \frac{1}{2}OB \cdot AH + \frac{1}{2}OB \cdot OD$
 $\frac{1}{2}OD \cdot OA \cdot \sin \phi = \frac{1}{2}OB \cdot OA \cos \phi + \frac{1}{2}OB \cdot OD$
 Dividing on both sides by $\frac{1}{2}OA \cdot OB \cdot OD$
 $\frac{\sin \phi}{OB} = \frac{\cos \phi}{OD} + \frac{1}{OA}$

$$\tan \lambda = -\cot \alpha_x \cos \phi + \cot \alpha_y \sin \phi$$



For $T=1$
 $OA = \cot \lambda$
 $OB = \tan \alpha_y$
 $OC = \tan \alpha_o$
 $OD = \tan \alpha_x$
 $OM = \tan \alpha_m$

Assignment-1

- Prove by Master Line Method

- (i) $\cot \alpha_o = \cot \alpha_x \sin \phi + \cot \alpha_y \cos \phi$
- (ii) $\tan \lambda = -\cot \alpha_x \cos \phi + \cot \alpha_y \sin \phi$
- (iii) $\cot \alpha_x = \cot \alpha_o \sin \phi - \tan \lambda \cos \phi$
- (iv) $\cot \alpha_y = \cot \alpha_o \cos \phi + \tan \lambda \sin \phi$
- (v) $\cot \alpha_m = \sqrt{\cot^2 \alpha_o + \tan^2 \lambda}$
- (vi) $\phi_\alpha = \phi - \tan^{-1} \left(\frac{\tan \alpha_o}{\cot \lambda} \right)$

- (i) $\tan \gamma_o = \tan \gamma_x \sin \phi + \tan \gamma_y \cos \phi$
- (ii) $\tan \lambda = -\tan \gamma_x \cos \phi + \tan \gamma_y \sin \phi$
- (iii) $\tan \gamma_x = \tan \gamma_o \sin \phi - \tan \lambda \cos \phi$
- (iv) $\tan \gamma_y = \tan \gamma_o \cos \phi + \tan \lambda \sin \phi$
- (v) $\tan \gamma_m = \sqrt{\tan^2 \gamma_o + \tan^2 \lambda}$
- (vi) $\phi_\gamma = \phi - \tan^{-1} \left(\frac{\tan \lambda}{\tan \gamma_o} \right)$

Reference:

LM-04-Conversion of tool angles from one system to another.pdf -pages 1-10